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Efficient Handling of Non-response in Sample Surveys: Development of Ratio-type Variance Estimators

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Author's contribution

The sole author designed, analyzed, interpreted and prepared the manuscript.

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ABSTRACT

The present study has been under taken to address the issue of presence and absence of nonresponse problems in Sample surveys. We have developed some new efficient ratio-type variance estimators for the computation of the finite population variance in presence and absence of nonresponse, by incorporating Positional parameters as auxiliary information. The expression for mean square errors of proposed estimators has been derived up to the first order of approximation. To test the efficiency of new developed estimators, practical demonstration has been carried to ascertain the performance of suggested Estimators.

Keywords: Bias; MSE_{mim}; sample random sampling; quartiles; deciles, trimmed meanand efficiency.

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1. INTRODUCTION

"The problem of non-response from respondents in survey data is one of the biggest problems while ascertaining the information from the source. The most popular Sub-sampling scheme introduced by Hansen and Hurwitz in 1946 is widely used to handle the non-response problems in survey data. In our present study, we will adapt this sub-sampling technique to handle the non-response problems in survey data. The technique is based on two-way stratification, one for respondent group and the other for nonrespondent group in phase first of survey. Then in phase-II, by making intensive efforts, a sub sample from non-respondent strata is drawn to recover the non-response. The strategy of developing efficient estimators through proper utilization of supplementary information has been widely addressed by different authors, when the

strong association exists between the auxiliary variable and study variable". To enhance the efficiency of estimators in presence and absence of non-response by utilizing auxiliary information, different authors have searched different Estimators such as Isaki (Isaki, 1983) who has introduced ratio and regression estimators. Similarly, Upadhaya and Singh (Upadhaya and Singh, 1999) have used "coefficient of Kurtosis as supplementary information to improve the efficiency of Estimators". (Kadilar and Cingi, 2006a) used "coefficient of skewness. On the same lines, several authors have contributed their research efforts to improve the efficiency of estimators". From the present literature, the issue of non response problems in survey sampling is being regularly addressed by the authors such as Hansen and Hurwitz, 1946, Sarandal et el, 2005, Riaz et el., 2014, Singh et el, 2016 and Shahzad et e., 2017.

2. REVIEW OF ESTIMATORS IN LITERATURE

Let the finite population under survey be $Z = \{Z_1, Z_2, ..., Z_N\}$, which consists of N distinct and identifiable units. Let Y be a real variable with value Y_i measured on Z_i , i = 1, 2, 3, ..., N, giving a vector $Y = \{y_1, y_2, ..., y_N\}$. The aim of our effort is to estimate the populations mean $\overline{Y} = \frac{1}{N} \sum_{i=1}^{N} y_i$

and its variance $S_Y^2 = \frac{1}{N-1} \sum_{I=1}^{N} (y_i - \overline{y})^2$ on the basis of random sample selected from afinite

population Z .

2.1 Notations

 $N = population \quad size, n = sample \quad size,$ $\gamma = \frac{N-n}{n}, Y = Study \text{ var } iable, X = Auxiliary \text{ var } iable, \overline{X} \text{ and } \overline{Y} = Population \text{ means}$ $\overline{x} \text{ and } \overline{y} = Sample \text{ means}, S_{Y}^{2} \text{ and } S_{x}^{2} = Population \text{ var } iances$ $s_{y}^{2} \text{ and } s_{x}^{2} = Sample \text{ var } iances \quad C_{x} \text{ and } C_{y} = Cofficient \text{ of var } iations$ $\rho = Cofficient \text{ of } Correlation, \beta_{2(x)} = Cofficient \text{ of kurtosis}$ $\beta_{2(y)} = Cofficient \text{ of kurtosis}, \beta_{1(x)} \text{ and } \beta_{1(y)} = Coefficient \text{ of skewness}$ $Q_{1} = First \text{ quartile}, Q_{2} = 2^{nd} \text{ quartile } Q_{3} = 3^{rd} \text{ Quartile }, Q_{r} = Quartile \text{ range}, Q_{d} = Quartile \text{ deviation}$ $D_{1} = First \text{ Decile }, D_{2} = 2^{nd} \text{ Decile }, D_{3} = 3^{rd} \text{ DecileD}_{4} = 4^{th} \text{ Decile }, D_{5} = 5^{th} \text{ Decile } \text{ and } \lambda_{rs} = \frac{\mu_{rs}}{\mu_{rs}^{\frac{r}{2}} \mu_{rs}^{\frac{r}{2}}}$

3. EXISTING ESTIMATORS IN ABSENCE OF NON-RESPONSE FROM THE LITERATURE

3.1 Ratio Type Variance Estimator Proposed by ISAKI, 1983:

$$\hat{S}_{R_{1}}^{2} = s_{y}^{2} \frac{S_{x}^{2}}{s_{x}^{2}}$$

Bias $((\hat{S}_{R_{1}}^{2}) = \gamma S_{y}^{2} [(\beta_{2(x)} - 1) - (\lambda_{22} - 1)]$
MSE $((\hat{S}_{R_{1}}^{2}) = \gamma S_{y}^{4} [(\beta_{2(y)} - 1) + (\beta_{2(x)} - 1) - 2(\lambda_{22} - 1)]$

3.2 Ratio Type Variance Estimator Proposed by Upadhaya and Singh, 1999:

$$\hat{S}_{R_{2}}^{2} = s_{y}^{2} \left[\frac{S_{x}^{2} + \beta_{2x}}{s_{x}^{2} + \beta_{2x}} \right]$$

Bias $((\hat{S}_{R_{2}}^{2}) = \gamma S_{y}^{2} \theta_{2} \left[\theta_{2} (\beta_{2(x)} - 1) - (\lambda_{22} - 1) \right]$
MSE $((\hat{S}_{R_{2}}^{2}) = \gamma S_{y}^{4} \left[(\beta_{2(y)} - 1) + \theta_{2}^{2} (\beta_{2(x)} - 1) - 2\theta_{2} (\lambda_{22} - 1) \right]$

3.3 Ratio Type Variance Estimator Proposed by Kadilar and Cingi, 2006a:

$$\begin{split} \hat{S}_{R_{3}}^{2} &= s_{y}^{2} \left[\frac{S_{x}^{2} + C_{x}}{s_{x}^{2} + C_{x}} \right] \\ \text{Bias}\left((\hat{S}_{R_{3}}^{2}) = \gamma S_{y}^{2} \tau_{3} \left[\tau_{3} (\beta_{2(x)} - 1) - (\lambda_{22} - 1) \right] \\ \text{MSE}\left((\hat{S}_{R_{3}}^{2}) = \gamma S_{y}^{4} \left[(\beta_{2(y)} - 1) + \tau_{3}^{2} (\beta_{2(x)} - 1) - 2\tau_{3} (\lambda_{22} - 1) \right] \end{split}$$

3.4 Ratio Type Variance Estimator Proposed by Singh et al., 2016:

$$\hat{S}_{R_4}^2 = s_y^2 \left[\frac{S_x^2 + Q_1^2}{s_x^2 + Q_1^2} \right]$$

Bias
$$((\hat{S}_{R_4}^2) = \gamma S_y^2 \omega_4 \left[\omega_4 (\beta_{2(x)} - 1) - (\lambda_{22} - 1) \right]$$

MSE $((\hat{S}_{R_4}^2) = \gamma S_y^4 \left[(\beta_{2(y)} - 1) + \omega_4^2 (\beta_{2(x)} - 1) - 2\omega_4 (\lambda_{22} - 1) \right]$

Remark :" θ_2 , τ_3 and ω_4 " are Constants

 R_i 'Stands for ratio estimator and i = 1,2,3,4

4. PROPOSED ESTIMATORS

1.
$$\hat{S}_{R_{1}}^{2} = Ks_{y}^{2} \left[\frac{S_{x}^{2} + (\beta_{1x}) \times (D_{3})^{2}}{s_{x}^{2} + (\beta_{1x}) \times (D_{3})^{2}} \right]$$

2. $\hat{S}_{R_{2}}^{2} = Ks_{y}^{2} \left[\frac{S_{x}^{2} + (\beta_{1x}) \times (D_{4})^{2}}{s_{x}^{2} + (\beta_{1x}) \times (D_{4})^{2}} \right]$
3. $\hat{S}_{R_{3}}^{2} = Ks_{y}^{2} \left[\frac{S_{x}^{2} + (\beta_{1x}) \times (D_{5})^{2}}{s_{x}^{2} + (\beta_{1x}) \times (D_{5})^{2}} \right]$

Where 'K' is Characterizing scalar to be determined such that the MSE of the proposed estimators is minimized.

4.1 The Bias and Mean Square Error of Proposed Estimators up to First Order Approximation has been Carried out by the Following Expression

Let
$$e_0 = \frac{s_y^2 - S_y^2}{S_y^2}$$
 and $e_1 = \frac{s_x^2 - S_x^2}{S_x^2}$. Further we can write $s_y^2 = S_y^2(1 + e_0)$ and $s_x^2 = S_x^2(1 + e_1)$

and from the definition of e_0 and e_1 we obtain:

$$E[e_0] = E[e_1] = 0, E[e_0^2] = \frac{1-f}{n}(\beta_{2(y)} - 1), E[e_1^2] = \frac{1-f}{n}(\beta_{2(x)} - 1), E[e_0e_1] = \frac{1-f}{n}(\lambda_{22} - 1)$$

The proposed estimator can be written as:

$$\hat{R}_{MS} = K s_{y}^{2} (1 + e_{0}) (1 + R_{i} e_{1})^{-1}$$
(1)

Expanding the right hand side of above equation up to the first order approximation we get

$$\hat{R}_{MS} = Ks_{y}^{2}(1 + e_{0} - R_{i}e_{1} - R_{i}e_{0}e_{1} + R_{i}^{2}e_{1}^{2})$$
⁽²⁾

After subtracting the population variance S_{v}^{2} of study variable on both sides of above equation we get

$$\hat{R}_{MS} - S_{y}^{2} = KS_{y}^{2}(1 + e_{0} - R_{i}e_{1} - R_{i}e_{0}e_{1} + R_{i}^{2}e_{1}^{2}) - S_{y}^{2}$$
(3)

By taking expectations on both sides of above equation, we get the bias of the proposed estimators;

Bias =
$$\gamma KS_{y}^{2}R_{i}[R_{i}(\beta_{2x}-1)-R_{i}(\lambda_{22}-1)]+S_{y}^{2}(K-1)$$
 (4)

The mean square error is obtained by squaring both sides of equation (4.5) and taking expectations on both sides up to first order of approximation as:-

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$$MSE = S_{y}^{4} \left[K^{2} \gamma (\beta_{2y} - 1)' + (3K^{2} - 2k) R_{i}^{2} (\beta_{2x} - 1) - 2(2K^{2} - K) R_{i} \gamma (\lambda_{22} - 1) + (K - 1)^{2} \right]$$
(5)
Where $\gamma = \frac{1 - f}{n}$, MSE is minimum for $K = \frac{1 + R_{i}^{2} \gamma (\beta_{2x} - 1) - R_{i} \gamma (\lambda_{22} - 1)}{1 + \gamma (\beta_{2y} - 1)' + 3R_{i}^{2} \gamma (\beta_{2x} - 1) - 4R_{i} \gamma (\lambda_{22} - 1)}$

The Minimum MSE for the estimator, optimum value of K is :

$$MSE_{\min} \hat{R}_{MS} = S_{y}^{4} \left[1 - \frac{\left\{ \left(1 + R_{i}^{2} \gamma (\beta_{2x} - 1) - R_{i} \gamma (\lambda_{22} - 1) \right)^{2} \right\} \right\}}{1 + \gamma (\beta_{2y} - 1) + 3R_{i}^{2} \gamma (\beta_{2x} - 1) - 4R_{i} \gamma (\lambda_{22} - 1)} \right]$$

$$Where, (\beta_{2y} - 1) = (\beta_{2y} - 1)'$$
(6)

5. NUMERICAL ILLUSTRATION

We use the data set presented in Sarandal*et al.* (1992) "concerning (P85) 1985 population considered as Y and RMT85 revenue from 1985 municipal taxation in millions of kronor considered as X". Descriptive statistics is given below:

$$N = 234, n = 35, \overline{Y} = 29.3626, \overline{X} = 245.088, S_y = 51.556, S_x = 596.332, \rho = 0.96, \beta_{2y} = 89.231, \beta_{2x} = 89.189$$

$$\lambda_{22} = 4.041, \beta_{1x} = 8.83, \beta_{1y} = 8.27, TM = 167.4, Q_1 = 67.75, Q_2 = 113.5, Q_3 = 230.25, C_x = 2.43, D_1 = 49.0, D_2 = 63.0, D_3 = 75.0, D_4 = 90.0, D_5 = 113.5, D_6 = 145.9, D_7 = 197.9, D_8 = 271.1, D_9 = 467.5, D_{10} = 6720.0$$

We consider 20% weight for non-response (missing values) and have considered last 47 values as non-respondents results are as follows:-

$$l = 2, S_{y_2}^2 = 2.9167, \beta_2(y_2) = 11.775, N_2 = 47$$

Table 1. Mean square error of existing estimators and proposed estimators in absence of nonresponse

Existing Estimators	Mean square error	
Isaki, 1983	29216846.22	
Upadhyaya and Singh, 1999	29187686.03	
Kadilar and Cingi, 2006a	29216846.22	
Singh <i>et al., 19</i> 46	28839478.44	
Proposed [1]	993482.49	
Proposed[2]	1368635.80	
Proposed [3]	1960434.83	

Table 2. Percent relative efficiency of existing and proposed estimators in absence of non-
response

Existing estimators → Proposed estimators↓	Isaki, 1983	Upadhyaya and Singh, 1999	Singh <i>et al.,</i> 2016
Proposed [1]	2940 %	2937 %	2902 %
Proposed[2]	2134 %	2132 %	2107 %
Proposed [3]	1490 %	1488 %	4171 %

5.1 Existing Estimators in Presence of Non-response

Hansen and Hurwitz, 1946 "sub sampling scheme is the most popular scheme, used for the Nonresponse problems let us consider a finite population consisting of *N* units. Let *y* be the character under study and a simple random sample of size *n* is drawn without replacement, of which n_1 units respond and n_2 units do not respond". From the n_2 non-respondents we select a sample of size

 $r = \frac{n_2}{k}$, $(k \ge 1)$ where k is the inverse sampling rate at the second phase sample of size n (fixed in advance) and from whom we collect the required information. It is assumed here that all the r units respond fully this time.

Let N_1 and $N_2 = N - N_1$ be the sizes of the responding and non-responding units from the finite population $N; W_1 = \frac{N_1}{N}, W_2 = \frac{N_2}{N}$ are the corresponding weights

Hansen and Hurwitz (1946) unbiased estimator under non-response is given by

$$Var(\hat{T}') = S_y^4(\beta_{2y} - 1) + WS_{y2}^4\beta_2(y_2)^* \text{ where } W = \frac{N_2(l-1)}{nN}, \text{ Where, } I = \text{sampling inverse rate}$$

5.2 Ratio Type Variance Estimator Proposed by Isaki, 1983

$$\hat{S}_{Is}^{2} = s_{y}^{\prime 2} \left[\frac{S_{x}^{2}}{s_{x}^{2}} \right]$$
(7)

The bias and mean square error of the estimator up to first order of approximation is given by the following expression

Bias
$$(\hat{S}_{IS}^{2}) = \gamma S_{y}^{2} \left[(\beta_{2(x)} - 1)' - (\lambda_{22} - 1) \right]$$
 (8)

$$\mathsf{MSE}((\hat{S}_{IS}^{2}) = \gamma S_{y}^{4} \left[(\beta_{2(y)} - 1)' + (\beta_{2(x)} - 1) - 2(\lambda_{22} - 1) \right]$$
(9)

Where,
$$(\beta_{2y} - 1)' = (\beta_{2y} - 1) + \frac{WS_{y2}^{4}(\beta_{2y})^{*}}{S_{y}^{4}} = \frac{Var(\hat{T}')}{S_{y}^{4}}$$

5.3 Ratio Type Variance Estimator Proposed by Upadhyaya and Singh, 1999

$$\hat{S}_{US}^{2} = s_{y}^{\prime 2} \left[\frac{S_{x}^{2} + \beta_{2}(x)}{s_{x}^{2} + \beta_{2}(x)} \right]$$
(10)

The bias and mean square error of the estimator up to first order of approximation is give the following expression

Bias
$$((\hat{S}_{US}^{2}) = \gamma S_{y}^{2} A_{US} \left[A_{US} \left(\beta_{2(x)} - 1 \right)' - (\lambda_{22} - 1) \right]$$
 (11)

$$\mathsf{MSE}\left(\left(\hat{S}_{US}^{2}\right) = \gamma S_{y}^{4} \left[\left(\beta_{2(y)} - 1\right)' + A_{US}^{2} \left(\beta_{2(x)} - 1\right) - 2A_{US} \left(\lambda_{22} - 1\right)\right]$$
(12)

Where
$$(\beta_{2y} - 1)' = (\beta_{2y} - 1) + \frac{WS_{y2}^4(\beta_{2y})^*}{S_y^4} = \frac{Var(\hat{T}')}{S_y^4}$$

5.4 Ratio Type Variance Estimator Proposed by Singh et al., 2016

$$\hat{S}_{s}^{2} = s_{y}^{\prime 2} \left[\frac{S_{x}^{2} + Q_{1}^{2}}{s_{x}^{2} + Q_{1}^{2}} \right]$$
(13)

The bias and mean square error of the estimator up to first order of approximation is given by the following expression

Bias
$$((\hat{S}_{s}^{2}) = \gamma S_{y}^{2} A_{1} \left[A_{s} (\beta_{2(x)} - 1)' - (\lambda_{22} - 1) \right]$$
 (14)

$$\mathsf{MSE}((\hat{S}_{s}^{2}) = \gamma S_{y}^{4} \left[(\beta_{2(y)} - 1)' + A_{s}^{2} (\beta_{2(x)} - 1) - 2A_{s} (\lambda_{22} - 1) \right]$$
(15)

Where
$$(\beta_{2y} - 1)' = (\beta_{2y} - 1) + \frac{WS_{y2}^{4}(\beta_{2y})^{*}}{S_{y}^{4}} = \frac{Var(\hat{T}')}{S_{y}^{4}}$$

6. PROPOSED ESTIMATORS IN PRESENCE OF NON-RESPONSE

$$1. \ \hat{S}_{R_{1}}^{2} = Ks_{y}^{2} \left[\frac{S_{x}^{2} + (\beta_{1x}) \times (D_{3})^{2}}{s_{x}^{2} + (\beta_{1x}) \times (D_{3})^{2}} \right], 2. \ \hat{S}_{R_{1}}^{2} = Ks_{y}^{2} \left[\frac{S_{x}^{2} + (\beta_{1x}) \times (D_{4})^{2}}{s_{x}^{2} + (\beta_{1x}) \times (D_{4})^{2}} \right],$$
$$3. \ \hat{S}_{R_{1}}^{2} = Ks_{y}^{2} \left[\frac{S_{x}^{2} + (\beta_{1x}) \times (D_{5})^{2}}{s_{x}^{2} + (\beta_{1x}) \times (D_{5})^{2}} \right]$$

where 'K' is a Characterizing scalar to be determined such that the MSE of the proposed estimators is minimized. The bias and mean square error of the proposed estimators has been carried out by the following mathematical

Table 3. Mean square errors of existing estimators in presence of non response

Existing estimators	Mean square error	
Isaki, 1983	29215130.96	
Upadhyaya and Singh, 1999	29185970.72	
Singh et al., 2016	28837763.13	

Table 4. Mean square errors of proposed estimators in presence of non res	ponse
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Proposed estimators	Mean square error
$\hat{S}_{p_1}^2 = K {s'_y}^2 \left[\frac{S_x^2 + (\beta_{1x})(D_3)^2}{s_x^2 + (\beta_{1x})(D_3)^2} \right]$	661069.84
$\hat{S}_{p_1}^2 = K {s'_y}^2 \left[\frac{S_x^2 + (\beta_{1x})(D_4)^2}{s_x^2 + (\beta_{1x})(D_4)^2} \right]$	1083247.49
$\hat{S}_{p_1}^2 = K {s'_y}^2 \left[\frac{S_x^2 + (\beta_{1x})(D_5)^2}{s_x^2 + (\beta_{1x})(D_5)^2} \right]$	2497795.24

ExistingProposedEstimators \rightarrow Estimators \downarrow	Isaki,1983	Upadhyaya and Singh 1999	, Singh et al., 2016
$\hat{S}_{p_1}^2 = K s_y'^2 \left[\frac{S_x^2 + (\beta_{1x})(D_3)^2}{s_x^2 + (\beta_{1x})(D_3)^2} \right]$	4419.37 %	4414.96 %	4362.28 %
$\hat{S}_{p_1}^2 = K s_y'^2 \left[\frac{S_x^2 + (\beta_{1x})(D_4)^2}{s_x^2 + (\beta_{1x})(D_4)^2} \right]$	2696.99 %	2694.30 %	2662.15 %
$\hat{S}_{p_1}^2 = K s_y'^2 \left[\frac{S_x^2 + (\beta_{1x})(D_5)^2}{s_x^2 + (\beta_{1x})(D_5)^2} \right]$	1169.63 %	1168.46 %	1154,52 %

Table 5. Percent relative efficiency of existing estimators with proposed estimators inPresence of non-response

7. CONCLUSION

In this manuscript, suggested estimators for the estimation of finite population variance in absence and presence of non-response have clearly determined that proposed Estimators have shown excellent performance over the Existing Estimators, which can be easily accessed from the tables viz, Table 1, Table 2, Table 3, Table 4, Table 5. Hence suggested estimators may be preferred over existing estimators.

DISCLAIMER (ARTIFICIAL INTELLIGENCE)

Author(s) hereby declare that NO generative AI technologies such as Large Language Models (ChatGPT, COPILOT, etc) and text-to-image generators have been used during writing or editing of this manuscript.

COMPETING INTERESTS

Author has declared that no competing interests exist.

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