

# The Signature of a Windy Radio Supernova Progenitor in a Binary System

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# Abstract

Type II supernova progenitors are expected to emit copious amounts of mass in a dense stellar wind prior to the explosion. When the progenitor is a member of a binary, the orbital motion modulates the density of this wind. When the progenitor explodes, the high-velocity ejecta collides with the modulated wind, which in turn produces a modulated radio signal. In this Letter we derive general analytic relations between the parameters of the radio signal modulations and binary parameter in the limit of large member-mass ratio. We use these relations to infer the semimajor axis of SN 1979c and a lower bound for the mass of the companion. We further constrain the analytic estimates by numerical simulations using the Astrophysical Multipurpose Software Environment framework. In these calculations we simulate the progenitor binary system including the wind and the gravitational effect of a companion star. The simulation output is compared to the observed radio signal in supernova SN 1979C. We find that it must have been a binary with an orbital period of about 2000 yr. If the exploding star evolved from a  $\sim$ 18  $M_{\odot}$  zero-age main sequence at solar metallicity, we derive a companion mass of 5–12  $M_{\odot}$  in an orbit with an eccentricity lower than about 0.8.

Key words: stars: massive – stars: winds, outflows – supernovae: general

#### 1. Introduction

One of the open questions in stellar astrophysics concerns the identity and properties of supernova progenitors (Smartt [2009](#page-4-0); Maeda & Terada [2016](#page-4-0)). Despite the large number of supernovae detected, little can be inferred about the progenitors because peak luminosities occur after the progenitor has exploded. In some rare cases the progenitor of a nearby supernova can be identified from archival data (Van Dyk [2017](#page-4-0)). Based on population studies, many supernova progenitors have a companion that can alter the progenitor's evolutionary track (Portegies Zwart & Heuvel [1999](#page-4-0); Sana et al. [2012](#page-4-0)).

In this Letter we describe a method for inferring information not just about the progenitor, but also about its binary companion and its orbit. Some supernova progenitors emit copious amount of stellar wind prior to the explosion (Heuvel & Portegies Zwart [2013;](#page-4-0) Moriya et al. [2014](#page-4-0)). The motion of the progenitor around the center of mass modulates the wind, increasing the density in the forward direction (relative to the velocity of the progenitor) and reducing it in the backward direction (see also Ishii et al. [1993](#page-4-0); Saladino et al. [2018](#page-4-0)). When the progenitor explodes, the ejecta collide with the ripples in the wind and launch a shock wave. A fraction of the thermal energy in the shock is converted into magnetic fields and suprathermal electrons. These relativistic electrons gyrate in the magnetic fields and emit synchrotron radiation in radio (Chevalier [1998](#page-4-0)). As a result of the modulation in the wind, the flux of the radio emission will also fluctuate. In this Letter we relate the fluctuation in radio to the density modulation in the wind, and then to the properties of the progenitor binary system.

Fluctuations in the radio have been measured for SN 1979c (Weiler et al. [1991](#page-4-0)). This supernova has been followed up for about 10 years, and during that period the radio flux fluctuated with a period of about 4 years, and a relative amplitude of about 0.1. Based on later X-ray observations it was suggested that the remnant of the supernova is a 5–10  $M_{\odot}$  black hole

(Patnaude et al. [2009](#page-4-0)), and the mass of the progenitor is estimated at  $18 \pm 3 M_{\odot}$ . The mass loss rate close to the explosion time was estimated at  $\sim$ 1.2 × 10<sup>-4</sup> M<sub>☉</sub> yr<sup>-1</sup> (Weiler et al. [1991](#page-4-0)). With such conditions, SN 1979c is a good test case to demonstrate how binary parameters can be inferred from variations in the observed radio signal.

This Letter is organized as follows. In the next section we derive the analytic formalism that we apply in Section [3](#page-1-0) to the observed supernova SN 1979C. In Section [4](#page-1-0) this formalism is tested by means of simulations, and we conclude in Section [5](#page-3-0).

#### 2. Analytic Estimates

Let us consider two stars with masses  $M \gg m$  in a binary with orbital period  $P_{\text{orb}}$ . The stars are assumed to move on circular orbits ( $e = 0$ ) with a semimajor axis a and observed edge on. The period is given by

$$
P_{\rm orb} = 2\pi \sqrt{\frac{a^3}{G(M+m)}}.
$$
 (1)

The radius of the orbit of the massive star is  $am/M$ , and therefore its orbital velocity is

$$
v_M = \frac{m}{M} \sqrt{\frac{G(M+m)}{a}}.
$$
 (2)

We also assume that the more massive member emits a wind at velocity  $v_w$ . The relative amplitude of the density of the wind due to the motion of the massive companion scales with the ratio of orbital to wind velocity

$$
\frac{\delta \rho}{\rho} \approx \frac{v_M}{v_w}.\tag{3}
$$

Now let us consider what happens when companion M explodes. We assume that, as a result of the explosion, the ejecta expand as a spherical shell moving at  $v_e \gg v_w$  and collide with previously emitted wind. As a result, a shock wave

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emerges and travels into the wind with a velocity comparable to  $v_e$ . This shock emits in the radio, and the strength of the emission oscillates with the upstream density. As the ejecta travel faster then the wind, the observed period of the oscillations will be smaller than the orbital period

$$
P_{\rm obs} \approx P_{\rm orb} \frac{v_w}{v_e}.\tag{4}
$$

If we assume that the relative fluctuations in flux are comparable to the fluctuations in density, we get

$$
\frac{\delta f}{f} \approx \frac{v_M}{v_w}.\tag{5}
$$

In the limit of a small secondary  $M \gg m$ , we can invert Equations  $(4)$  and  $(5)$  to get the secondary mass and separation

$$
a \approx \left(\frac{P_{\text{obs}}}{2\pi} \frac{v_e}{v_w}\right)^{2/3} (GM)^{1/3},\tag{6}
$$

$$
m \approx M \frac{\delta f}{f} \left( \frac{P_{\text{obs}} v_{w}^{2} v_{e}}{2\pi GM} \right)^{1/3}.
$$
 (7)

#### 2.1. Synchrotron Emission

In this section we calculate the prefactor of Equation  $(5)$ . To do so, we assume that the emission is due to synchrotron emission (Rybicki & Lightman [1979](#page-4-0)), where the generation of magnetic field and acceleration of particles to relativistic energies consumes a certain fraction of the downstream thermal energy (Chevalier [1998](#page-4-0)). The net energy flux per particle is given by

$$
L_s \approx B^2 r_e^2 c \gamma^2, \tag{8}
$$

where  $B$  is the magnetic field,  $r_e$  is the classical electron radius, c is the speed of light, and  $\gamma$  is the Lorentz factor of the electron. Most of the energy is emitted at the synchrotron frequency

$$
\omega_s \approx \frac{qB}{m_e c} \gamma^2 \tag{9}
$$

where q is the electron charge, and  $m_e$  is its mass. The magnetic energy is assumed to be a fixed fraction of the thermal energy, so  $B^2 \propto \rho v_e^2$ . The net luminosity per unit frequency therefore changes as

$$
L \propto \rho L/\omega_s \propto \rho^{3/2}.
$$
 (10)

Therefore, the relation between the relative changes in observed flux to relative changes in density is

$$
\frac{\delta f}{f} \approx \frac{3}{2} \frac{\delta \rho}{\rho}.\tag{11}
$$

#### 3. Application to SN 1979c

If we assume zero inclination and zero eccentricity, and a large ratio between the members of the binary, we can use Equations  $(6)$  and  $(7)$  to estimate the semimajor axis of the binary system and the mass of the star accompanying the supernova progenitor

$$
a \approx 430 \tilde{P}_{\rm obs}^{2/3} \tilde{v}_e^{-2/3} \tilde{v}_w^{2/3} \tilde{M}^{1/3} \text{ au},\tag{12}
$$

$$
m \approx 6\tilde{F}\tilde{M}^{2/3}\tilde{P}_{\rm obs}^{1/3}\tilde{v}_w^{2/3}\tilde{v}_e^{1/3}M_\odot,
$$
 (13)

where  $\tilde{P}_{\rm obs} = P_{\rm obs}/4 \text{ yr}, \tilde{v}_e \approx v_e/10^4 \text{ km s}^{-1}, \tilde{v}_w \approx v_w/20 \text{ km s}^{-1},$  $\tilde{M} = M/20 M_{\odot}$  and  $\tilde{F} = 10 \cdot \delta f/f$ .

We note that the mass obtained here is only a lower limit on the actual companion mass. Inclination can reduce the apparent amplitude of the radio oscillation by a factor  $\propto \cos i$ . Because our expression for the mass scales with the apparent amplitude of the radio oscillation, the real mass of the companion star may be larger than the estimated mass by a similar factor. However, as we demonstrate in the next section this factor does not propagate linearly into the mass estimate.

#### 4. Simulations

Having derived first-order estimates for the binary parameters that could lead to the observed ripples in the radio flux for SN 1979C, we now perform a series of simulations in which we verify some of the earlier analytical estimates and further constrain the parameters of the progenitor system. For this purpose we simulate the binary system prior to the supernova, assuming that the supernova blast wave interacting with the progenitor's wind is responsible for the observed fluctuations.

We simulated the wind evolution of the binary system over the 14,000 yr prior to the supernova. The simulations ware performed using the Astrophysical Multipurpose Software Environment (AMUSE; Portegies Zwart [2011;](#page-4-0) Portegies Zwart et al. [2012](#page-4-0), [2018](#page-4-0)). AMUSE is a component library for multiscale and multiphysics simulations. We set up our simulation using a binary system with an  $18 M_{\odot}$  Solar metallicity primary at zero age. The primary star was evolved for 9.6 Myr using the MESA (Paxton et al. [2010a](#page-4-0), [2010b](#page-4-0)) stellar evolution code at which time the star exhausted the central fuel in its  $5.27 M_{\odot}$  core. At this time the star has a luminosity of  $\sim$ 1.1 × 10<sup>4</sup>L<sub>⊙</sub>, a surface temperature of about 3500 K, and a mass loss rate in its wind of  $\sim 1.0 \times 10^{-4} M_{\odot} \,\mathrm{yr}^{-1}$ .

We ran simulations with companion masses 1, 3, 6, 9 12, or 15  $M_{\odot}$ . The companion star was evolved to the same age as the primary before putting it into a binary system. We performed several other calculations in which we varied the orbital period  $(P = 500, 1500, 1500, 2000, yr)$  and eccentricity ( $e = 0.15, 0.45,$ 0.60, 0.75 and  $e = 0.8$ ), but the results turn out to be rather insensitive to changes in the eccentricity or the companion mass.

We run the wind module in AMUSE, which was designed to simulate the slow accelerating wind of an AGB star (see Saladino et al. [2018;](#page-4-0) E. van der Helm et al. 2019, in preparation) with the  $Fi$  smoothed particles hydrodynamics solver (Gerritsen & Icke [1997](#page-4-0); Pelupessy et al. [2004](#page-4-0)). The integration of the equations of motion for the stars is realized using the Huayno symplectic N-body integrator (Pelupessy et al. [2012](#page-4-0)). The two codes are coupled with a bridge (Portegies Zwart et al. [2018](#page-4-0)) using a time step of 1 yr. We started the calculation with 50 smoothed-particle hydrodynamic (SPH) particles in a sphere around the primary star, and produce new particles at runtime with a mass of  $10^{-5} M_{\odot}$ . We performed additional simulations with  $10^{-6}$  and  $10^{-7} M_{\odot}$  per SPH particle, but the results are rather insensitive to the adopted resolution. In the highest resolution, however, we found interesting substructure

<span id="page-2-0"></span>

Figure 1. Face on (top) and edge on (bottom) view of the gas density distribution 14,000 yr after the beginning of wind injection. Both images are centered on the supernova progenitor. The primary (blue bullet) is a 18  $M_{\odot}$ supernova progenitor and the companion is a  $6 M_{\odot}$  (red bullet). The orbit is circular with a period of 2000 yr. The mass per SPH particle is  $10^{-5} M_{\odot}$ .

in the wind, probably due to turbulent motion, but for our comparison with the observations this is irrelevant. The particles are released in a homogeneous sphere with a radius of 100 au around the primary star, and ejected using to the accelerated wind model in AMUSE with an adopted terminal velocity of  $10 \text{ km s}^{-1}$  (which is consistent with the estimated velocity from the observations; Weiler et al. [1991](#page-4-0)). Due to internal pressure and the local heating by the primary star, the actual terminal velocity in the wind is sometimes hard to constrain, but will result naturally from the hydrodynamical simulation. As a consequence, the terminal velocity of the wind in the simulation is closer to 23 km s<sup>-1</sup>, which is consistent with known wind velocities of comparable progenitors (see for example, Beasor & Davies [2018](#page-4-0)).



Figure 2. 4.88 GHz radio flux as a function of time observed for SN 1979C (black bullets) taken directly from Figure 2 of Weiler et al. ([1991](#page-4-0)). The simulated curve is calculated using a  $6 M_{\odot}$  companion star in a circular orbit of 2000 yr. We shifted the curves to match them up with the observed radio flux (by  $\log \rho = 22.54$  in units of g cm<sup>-3</sup>). The first 5000 days after the onset of the supernova is corrected with a power law of index 1.6 to match up the baseline of the simulated curve with the observed radio flux  $S_{\nu}$ . We observed the binary in the orbital plane from apocenter. The time axis is obtained by dividing the distance from the supernova progenitor with the velocity of the supernova shell, for which we adopted  $v_{\rm sn} = 10^4$  km s<sup>-1</sup>.

We run the models for 14,000 yr producing snapshots every 100 yr. In Figure 1 we show the ripples caused by the stellar wind in the final shapshot using a  $6 M_{\odot}$  donor in a 2000 yr circular orbit. The relatively high mass, compared to our earlier estimate, was adopted because it turned out to produce an excellent comparison with the observed ripples, but similarly well-matching results could be obtained also for a lower-mass companion star.

Figure 2 shows the radio light curve inferred from the simulation. In this figure we view the binary in the plane of motion from the apocenter. From this viewing angle the simulation results seem to agree with the observation, but similar agreement can be achieved for different azimuthal angles. The red curve in Figure 2 is calculated using the mean of 100 SPH particles in a cylinder with 3000 au radius in the direction of the observer. We scaled the distance from the center of mass by the reciprocal of the velocity, such that each time represents the arrival time of the supernova ejecta to that distance, using a velocity of  $v_{\rm sn} = 10^4 \,\rm km\,s^{-1}$ .

We note that the periodic signal in the radio can only be observed in a limited range in time. Before roughly 1000 days, the radio emission is optically thick, in which case the flux is independent of the value of the density. After about 4000 days the ram pressure of the wind becomes comparable to the ambient pressure of the interstellar medium (ISM), which breaks our assumption of a freely expanding wind. Therefore, we only expect our model to fit the data between 1000 and 4000 days.

Comparing the observed radio data with the simulations is not trivial because of the confounding factors in the model. These confounding factors include the companion mass, inclination of the viewing angle, and the angle along the orbital plane. Changing the two angles introduces rotations in the spiral pattern, which causes a shift in the fluctuations. Changing the companion mass from about 3 to  $\sim$ 15  $M_{\odot}$  causes the density fluctuations in the wind to become more pronounced. However, the fluctuations in the density variations

<span id="page-3-0"></span>

Figure 3. Relative difference between the lowest value and the highest values of the density around the second bump at about 4000 days (see Figure [2](#page-2-0)). The dashed line gives the measured difference in the observations, and the bullet points represent the measurements from the simulations for circular orbits and viewed in the plane of motion from the apoapse at an age of 14,000 yr after the start of the simulation.

can be suppressed somewhat by changing the viewing angle. As a consequence, it turns out to be hard to constrain either the viewing angle or the companion mass.

To quantify the magnitude of the density contrast in the ripples we present in Figure 3 the relative height of the fluctuations  $\Delta S = 2 \frac{\rho_{\text{max}} - \rho}{\rho_{\text{max}} + \rho}$ -  $S = 2 \frac{\rho_{\text{max}} - \rho_{\text{min}}}{\rho_{\text{max}} + \rho_{\text{min}}}$  as a function of companion mass (from 1 to 25  $M_{\odot}$ ). Here for stars more massive than the primary we adopted a point mass, rather than an extended stellar object, because we expect stars that are more massive than the supernova progenitor to have collapsed to a black hole at an earlier epoch.

We further tested the effect of the initial eccentricity of the orbit, varying it from  $e = 0$  to  $e = 0.9$ . Up to an eccentricity of ~0.6, the results did not appreciably change, but higher eccentricities suppress the ripples at larger distances from the star. This is because the stars spend most of the time near the apocenter. In the high-resolution simulations some appreciable deviations from the spiral structure is noticeable when viewed directly from pericenter as respect to other viewing angles, but the effect is much smaller than the fluctuations in the radio observations. We therefore cannot constrain the binary eccentricity in the observations.

In Figure 4 we show the results of a few extra simulations in which we varied the companion mass and the orbital eccentricity. The density variations (and therefore also the fluctuations in radio) are rather pronounced in each of these cases. The intrinsic degeneracy in the problem in the inclination and orbital phase make it hard to constraint the orbital eccentricity or companion masses. The simulation with a shorter orbital period, however, shows more distinct peaks than the observations, and they do not line up nicely as is the case with the 2000 yr orbital period. But this parameter is degenerate in the velocity of the supernova ejecta.

# 5. Discussion and Conclusions

We propose that the ripples observed in the 4.88 and 1.47 GHz radio observations in SN 1979c result from the interaction between the stellar wind of the progenitor star and the supernova outflow. In that case, the observed ripples originate when the supernova outflow interacts with the slow



Figure 4. Comparison of four simulations with the same resulting but somewhat different parameters. The thick dark-gray curve gives the fit presented in Figure 3 of Montes et al. ([2000](#page-4-0)) to the radio data of Weiler et al. ([1991](#page-4-0)). As indicated in the top-right corner of the figure, we vary the companion mass of 1, 6, and 15  $M_{\odot}$  for circular orbits, as well as for one with an eccentricity of  $e = 0.75$ . All simulated binaries had an orbital period of 2000 yr, were performed at a resolution of  $10^{-5} M_{\odot}$  per SPH particle, and adopted a viewing angle in the plane of motion and along the binary's long axis (from the apocenter).

wind from the progenitor star. Density fluctuations in the wind then cause small variations in the radio flux. The observed variations then relate directly and linearly to density fluctuations in the interaction between the progenitor's wind and its supernova blast wave. We developed this hypothesis by deriving qualitatively the fluctuations in timescale, as well as the amplitude of the variations, and associate them to the range in possible binary companions masses and orbital periods.

We simulated the binary for 14,000 yr before the supernova explosion, taking the binary orbit and the wind produced by the supernova progenitor into account. For this purpose we couple a smoothed-particle hydrodynamics solver with a gravitational N-body code using the AMUSE software framework. The simulation results agree both with the observations and the theoretical analysis. In addition, the simulations allow us to consider cases where the companion mass is comparable to the primary. We cannot constrain the viewing angle, because this parameter is degenerate with the companion mass. The resulting signal is rather insensitive to the orbital eccentricity of the progenitor binary star. The best match with the observations is obtained for a companion mass between  $5 M_{\odot}$  and about  $12 M_{\odot}$ in a ∼2000 yr binary with relatively low ( $e \lesssim 0.8$ ) eccentricity.

We conclude that the ripples observed in SN 1979c are a natural consequence of a supernova in a binary system. The orbital period, velocity of the stellar wind prior to the supernova, and the velocity of the supernova ejecta are directly derivable from the observed ripples in the radio flux. We can only place a lower bound on the mass of the companion star, because of degeneracy with inclination. We argue that a mass ratio of  $M/m \geq 0.3$  is sufficient to produce pronounced ripples in the stellar wind of the supernova progenitor. The viewing angle is hard to constrain.

The derived binary parameters for the progenitor of SN 1979c are rather common for massive stars, and many supernovae are expected to show similar ripples in their radio light curves. Those ripples are probably most pronounced between the moment the blast wave becomes optically thin (after about 1000 days) and the moment the density in the stellar wind becomes comparable to the background density (about ∼4000 days after the supernova

<span id="page-4-0"></span>explosion). The relation between the time between ripples gives a direct measurement of the binary period before the supernova. Unless better observational data becomes available, the amplitude of the fluctuations and the shape of the curves will be insufficient to further constrain the companion mass or the orbital eccentricity.

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