



# Modeling Interactions of Narrowband Large Amplitude Whistler-mode Waves with Electrons in the Solar Wind inside $\sim 0.3$ au and at 1 au Using a Particle Tracing Code

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## Abstract

The discovery of large amplitude narrowband whistler-mode waves at frequencies of tenths of the electron cyclotron frequency in large numbers both inside  $\sim 0.3$  au and at  $\sim 1$  au provides an answer to longstanding questions about scattering and energization of solar wind electrons. The waves can have rapid nonlinear interactions with electrons over a broad energy range. Counter propagation between electrons and waves is not required for resonance with the obliquely propagating waves in contrast to the case for parallel propagation. Using a full 3D particle tracing code, we have examined interactions of electrons with energies from 0 eV to 2 keV with whistler-mode waves with amplitudes of  $20 \text{ mV m}^{-1}$  and propagation angles from  $0^\circ$  to  $180^\circ$  to the background magnetic field. Interactions with wave packets and single waves are both modeled based on observations at  $\sim 0.3$  au and 1 au. A test particle simulation approach allows us to examine the particle motion in detail, which reveals kinetic effects of resonant interactions. The simulations demonstrate the key role played by these waves in rapid scattering and energization of electrons. Strong scattering and energization for some initial energy and pitch angle ranges occurs for both counter-propagating and obliquely propagating waves. Strong scattering of strahl electrons counteracts the pitch angle narrowing due to conservation of the first adiabatic invariant as electrons propagate from the Sun into regions of smaller magnetic field. Scattering also produces the hotter isotropic halo. The concomitant limiting of the electron heat flux is also relevant in other astrophysical settings.

*Unified Astronomy Thesaurus concepts:* Plasma physics (2089); Plasma astrophysics (1261); Solar physics (1476)

*Supporting material:* animations

## 1. Introduction

Many researchers have studied the evolution of solar wind electron distributions as they propagate away from the Sun. If only adiabatic effects are included, the field-aligned suprathermal strahl electrons would narrow in pitch angle with distance from the Sun, losing perpendicular energy as the magnetic field decreases to conserve the first adiabatic invariant. Instead, satellite observations from  $\sim 0.2$  to  $>5$  au have shown that the pitch angle width increases with radial distance (Maksimovic et al. 2005; Štverák et al. 2009; Halekas et al. 2020a), and that strahl may be completely scattered by  $\sim 5.5$  au (Graham et al. 2017). Because the strahl electrons carry the bulk of the heat flux, many studies are framed as determining the mechanisms that control the heat flux (Gary et al. 1994; Bale et al. 2013; Halekas et al. 2020b). Studies of strahl evolution and heat flux control have assessed the relative roles of Coulomb collisions and wave particle interactions, often concluding that the wave particle interactions are necessary (Phillips & Gosling 1990; Vocks 2012; Bale et al. 2013; Boldyrev & Horaites 2019).

Whistler-mode waves have frequently been invoked as a plausible mechanism to scatter the strahl because interactions with whistler-mode waves do not conserve the first adiabatic invariant since the wave frequency and electron gyrofrequency are comparable (Schulz & Lanzerotti 1974). Until recently most theoretical studies focused on waves propagating parallel to the solar wind magnetic field. For these waves, the resonance condition,  $\omega - \mathbf{k} \cdot \mathbf{v}_e = n\Omega_e$ , can only be satisfied if the

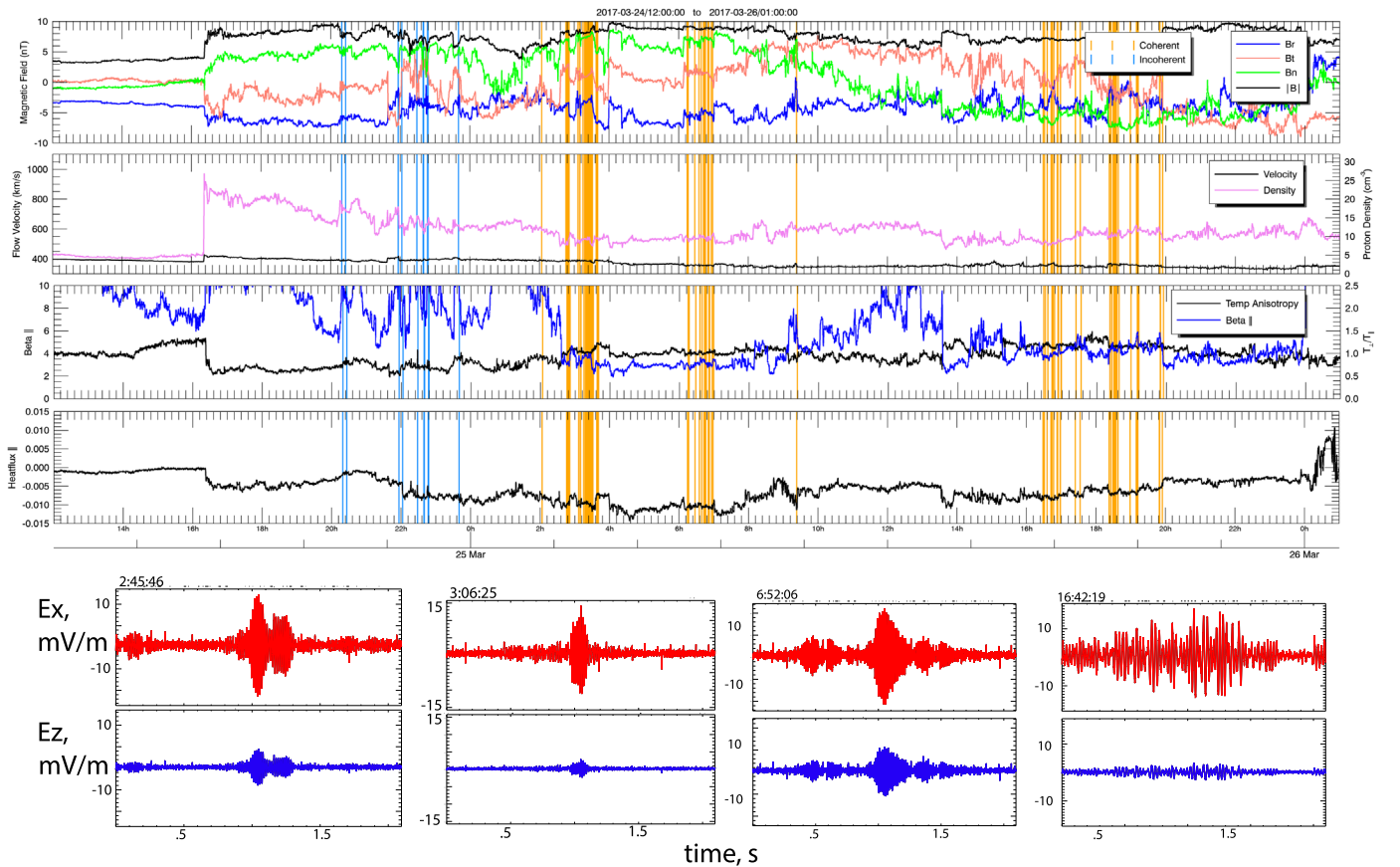
whistler-mode waves propagate sunward, opposite to the bulk of the electrons (Vocks et al. 2005; Gary & Saito 2007). If waves propagate anti-sunward, they can interact with only the small portion of the electrons that travel sunward.

Studies utilizing STEREO waveform capture data revealed the existence of large amplitude narrowband waves (NBWM) at frequencies of  $\sim 0.2 f_{ce}$  (electron cyclotron frequency) that propagate at large angles to the magnetic field ( $\sim 60^\circ$ – $65^\circ$ ) (Breneman et al. 2010; Cattell et al. 2020). The waves have electric field amplitudes ranging from 10 s up to  $>100 \text{ mV m}^{-1}$ :  $\sim 1$ – $3$  orders of magnitude larger than previously observed in the solar wind, with parallel components as much as 30% of the perpendicular component. For oblique waves, the resonance condition can be met for electrons and waves propagating in the same direction; thus the observations of large amplitude oblique waves opened up a more significant role for whistler-mode waves. Similar NBWM have been observed inside 0.3 au by the Parker Solar Probe (PSP; Agapitov et al. 2020; Cattell et al. 2021a) with more variable wave angles, including some wave packets that propagated sunward. Strahl electrons are strongly scattered by these waves over a broad energy range from  $\sim 100$  eV to  $\sim 1$  keV (Cattell et al. 2021b). Two recent particle-in-cell (PIC) simulations found that oblique whistlers were excited by the electron heat flux and strongly scattered electrons, one in the context of solar flares (Roberg-Clark et al. 2019) and one in the solar wind near 0.3 au (Micera et al. 2020).

In this report, we focus on the interaction of solar wind electrons with whistler-mode waves using a 3D particle tracing code with initial electron distributions and whistler properties based on those observed both at  $\sim 1$  au and inside  $\sim 0.3$  au enabling us to compare scattering in these two different



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**Figure 1.** Example of a CME with whistler-mode waves. (a) Magnetic field in RTN coordinates and magnitude; (b) solar wind velocity (black) and density (pink); (c) electron temperature anisotropy (black) and beta parallel (blue); and (d) parallel electron heat flux. Vertical blue lines are less coherent whistler-mode waves and vertical gold lines are narrowband whistler-mode waves (examples in bottom panels). Bottom: example 2.1 s waveform capture electric field, one perpendicular to the magnetic field component in red and one parallel component in blue.

regions. In Section 2, we show an example of a coronal mass ejection with the waves of interest, and briefly describe the particle tracing code. Section 3 shows the results obtained for interaction of electrons with energies from 0 eV to 2 keV, for both wave packets and a single wave. Section 4 discusses comparisons to previous studies and the implications of the results.

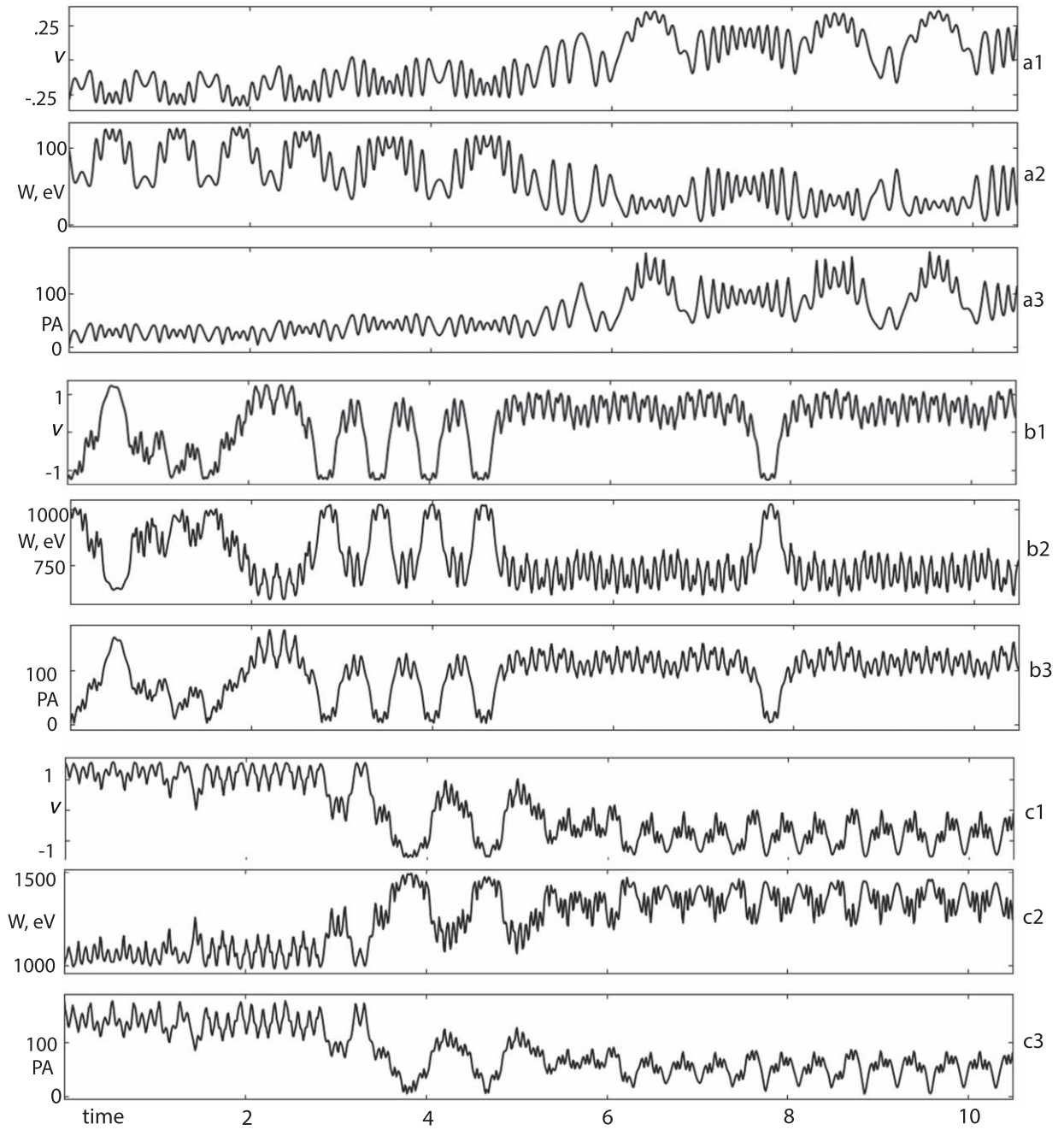
## 2. Whistler-mode Waves and Particle Tracing Study

An example of the association of the large amplitude oblique whistler-mode waves with solar wind structures at 1 au is shown in Figure 1, which plots a coronal mass ejection on 2017 March 24–25, identified as described in Jian et al. (2006) using data from the STEREO-A IMPACT (Luhmann et al. 2008) and S/Waves (Bougeret et al. 2008) instruments. The leading shock can be seen in the jump in the magnetic field in panel (a) and density in panel (b). Vertical blue lines are less coherent whistler-mode waves (see Cattell et al. 2020) and vertical gold lines are narrowband whistler-mode waves (examples in the bottom panels). The four example 2.1 s waveform capture electric fields, with one component perpendicular to the magnetic field in red and the parallel component in blue, show that the waves contain significant parallel electric fields, and that the waves occur in packets with durations of a few tenths of a second. Cattell et al. (2020) show a stream interaction region with similar close-packing of whistlers, and statistics including correlations to electron properties.

Inside  $\sim 0.3$  au, PSP data show that the narrowband whistlers are also often seen for many hours, usually occur in regions of smaller variable background magnetic fields, and are sometimes associated with magnetic field switchbacks (Agapitov et al. 2020; Cattell et al. 2021a, 2021b). Propagation angles range from near parallel, sometimes sunward propagating, to highly oblique. Average  $dB/B$  are  $\sim 0.05$  with values up to  $>0.12$ .

Utilizing a full 3D particle tracing code, with background magnetic fields, densities, and whistler-mode parameters based on the STEREO and PSP observations, we have examined the response of core, halo, and strahl electrons to the waves. Electrons with initial energies from 0 eV to 2 keV, pitch angles from  $0^\circ$  to  $180^\circ$ , and gyrophases of  $0^\circ$ – $360^\circ$  are traced. For the 0.3 au packet case, electrons up to 5 keV were traced to allow a direct comparison to the PIC simulations of Micera et al. (2020). Weighting of results is performed using electron parameters based on Wilson III et al. (2019) for 1 au, and on Halekas et al. (2020a) for inside 0.3 au.

The simulations utilize a 3D relativistic test particle code based on that of Roth et al. (1999) and Cattell et al. (2008), modified for solar wind magnetic field and density conditions. Results of an early version of the code (Breneman et al. 2010) showed prompt electron scattering, as much as  $30^\circ$ – $40^\circ$  in  $<0.1$  s, with energy changes also occurring. The current code is adapted for vectorized calculations of a distribution of test particles interacting with an input wave. The whistler waves are modeled in two different ways: (1) a single wave with a fixed



**Figure 2.** Time series for the interaction of an electron with a single wave propagating at  $65^\circ$  for three different electron initial conditions: (a) initial kinetic energy of 100 eV and initial pitch angle of  $0^\circ$ ; (b) initial energy of 1000 eV and pitch angle  $0^\circ$ ; and (c) initial energy of 1000 eV and pitch angle  $180^\circ$ . Time is normalized to wave periods. For each set of initial conditions the panels are from top to bottom: (1) the resonance mismatch; (2) the relativistic kinetic energy  $W$ ; and (3) the pitch angle.

frequency ( $0.15 f_{ce}$ ) and wave angle; and (2) a wave packet formed from 11 waves of varying frequencies. Wavelengths are determined from the cold plasma dispersion relation for a uniform plasma. In the simulation, we assume a uniform background field  $\mathbf{B} = B_0 \hat{z}$  and follow the motion of the electrons under the combined influence of the background magnetic field and the whistler-mode waves. The use of the uniform background magnetic field is justified because the interactions are rapid. In addition, the electrons making the largest excursions along the magnetic field travel distances over which the curvature of the field due to the Parker spiral is negligible.

In the energy range of interest, some particles cross multiple resonances in a short period of time (see Figure 2), as indicated by the resonance harmonic,  $\nu = \frac{\gamma}{\omega_{ce}(\omega - k_{\parallel} v_{\parallel})}$  (Roth et al. 1999). Due to the short-duration and frequent resonant interactions, the differential equations describing electron motion have phase space regions more significantly unstable than others, which makes the system sensitive to initial conditions. This requires more computational resources to solve numerically and to insure consistent solutions. Thus, instead of using the standard fourth-order Runge–Kutta integrator (as was used by Roth et al. 1999 and Breneman et al. 2010), we employ the Boris algorithm described in Ripperda et al. (2018). Solutions

calculated using the Boris method are known to be uniformly bounded in energy error (Qin et al. 2013), and thus able to calculate particle dynamics with great accuracy over a long simulation period. Additionally, we perform a variational calculation of the Lyapunov exponents at each time iteration such that the local phase space volume around the particles' trajectory is conserved to ensure the Boris algorithm's efficiency. Our code and the Hamiltonian analysis of the interactions are described in more detail in Vo (2021) and Vo et al. (2020).

We will show simulation results for two sets of parameters, one for 1 au ( $B_0 = 10$  nT and  $n = 5$  cm<sup>-3</sup> based on Cattell et al. 2020) and one for  $\sim 0.2$ – $0.3$  au ( $B_0 = 50$  nT and  $n = 300$  cm<sup>-3</sup> based on Cattell et al. 2021a). For the single wave cases,  $\frac{f}{f_{ce}} = 0.15$ , and we use three wave angles with respect to the background magnetic field,  $5^\circ$ ,  $65^\circ$ , and  $175^\circ$ . For the wave packets,  $\frac{f}{f_{ce}} = 0.15$  is the center frequency and the wave angles are  $0^\circ$ ,  $65^\circ$ , and  $180^\circ$ . For both, the electric field amplitude is  $20$  mV m<sup>-1</sup>.

### 3. Simulation Results

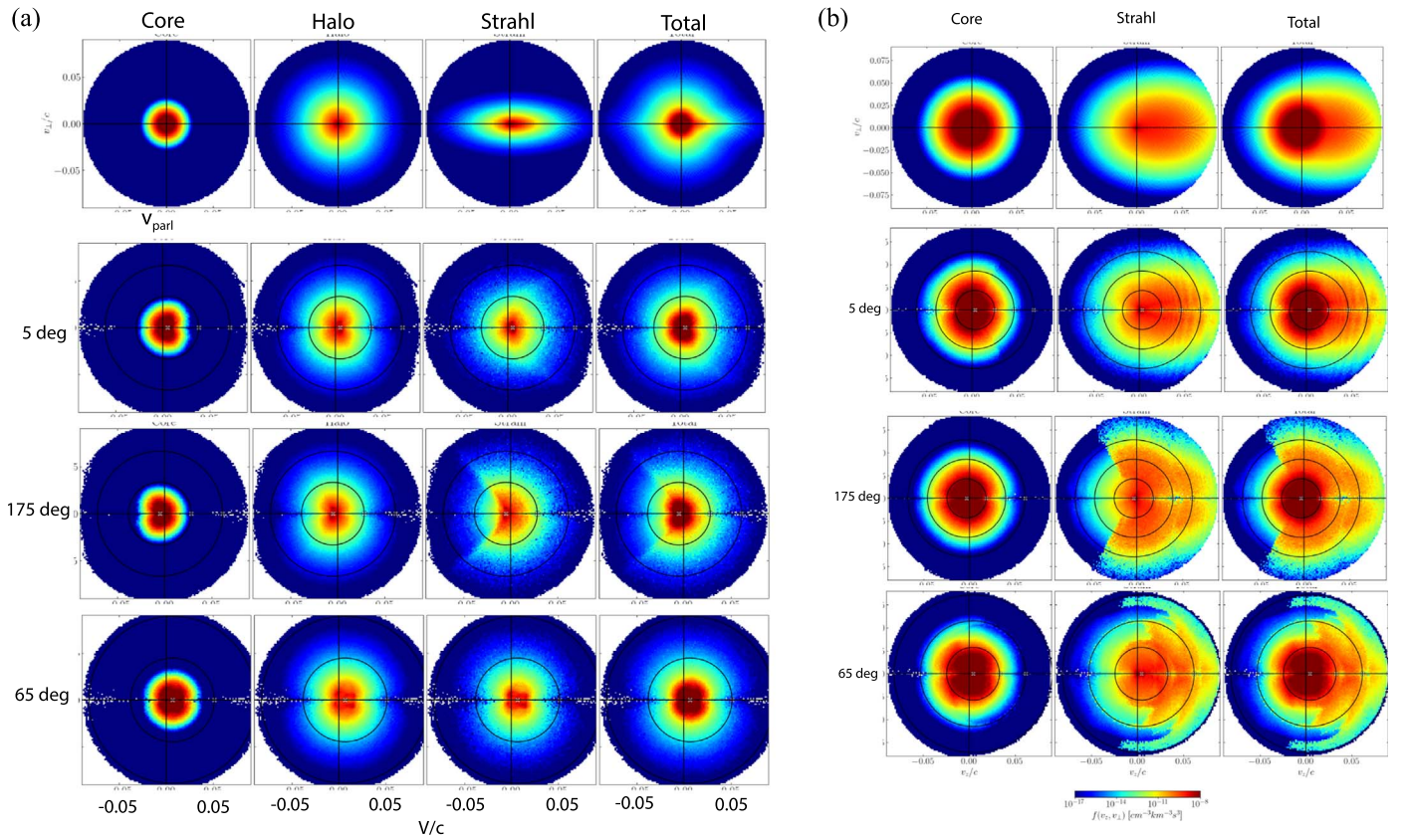
Examples of the interactions are shown in Figure 2, which plots the time series for three different electrons interacting with a single wave propagating at  $65^\circ$  using the 1 au parameters. From top to bottom the initial electron properties are (a) kinetic energy of 100 eV and pitch angle of  $0^\circ$ ; (b) kinetic energy of 1000 eV and pitch angle of  $0^\circ$ ; and (c) kinetic energy of 1000 eV and pitch angle of  $180^\circ$ . For each case, the panels plot (1) the resonance harmonic,  $\nu$ , (2) the relativistic kinetic energy  $W$  (in eV), and (3) the pitch angle. Time is normalized to wave periods. For clarity, only the first  $\sim 10$  wave periods are shown although simulations were run to  $\sim 60$  wave periods. In the 100 eV, initial pitch angle of  $0^\circ$  case (panels (a)), when the electron crosses the resonance line ( $\nu = 0$ ), the pitch angle increases to  $>100^\circ$ ; after subsequent interactions, the pitch angle averages  $\sim 100^\circ$ , and the energy is decreased to an average of  $\sim 40$  eV. In the 1000 eV, initial pitch angle of  $0^\circ$  case (panels (b)), the electron crosses the resonance line ( $\nu = 0$ ) multiple times with anticorrelated jumps in energy ( $\sim 300$ – $350$  eV) and pitch angle ( $\sim 80^\circ$  to  $>100^\circ$ ), settling at  $\sim 700$  eV and  $\sim 100^\circ$ . The 1000 eV electron with initial pitch angle of  $180^\circ$  (panels (c)) crosses the resonance at  $t \sim 3.5$ , with a rapid increase in energy to  $\sim 1400$  eV. After many other resonant interactions, the average energy is  $\sim 1300$  eV and the average pitch angle is  $\sim 50^\circ$ . The resonance harmonic reaches higher values as the electron initial energy increases, consistent with the operation of higher order resonances. In all three cases electrons are strongly scattered at the resonance crossing, and the change in pitch angle is anticorrelated with the change in energy as expected from theoretical models of scattering (Brice 1964; Kennel & Petschek 1966; Albert 2010). A detailed understanding of the interactions requires examination of resonance broadening and overlap for the specific wave parameters (Karimabadi et al. 1990, 1992), which is addressed in Vo (2021) and Vo et al. (2020).

The results for the full distributions for 1 au single wave cases after  $\sim 60$  wave periods are presented in Figure 3(a). All four panels show, from left to right, the core, halo, strahl, and total distribution, with the same color bars. The top panel shows the initial distribution, the second panel shows the

results for a wave angle of  $5^\circ$  (strahl velocity and wave phase velocity in the same direction), the third panel shows the results for a wave angle of  $175^\circ$  (strahl velocity and wave phase velocity in opposite directions), and the fourth panel shows the results for a wave angle of  $65^\circ$ , all at the simulation end time of  $\sim 60$  wave periods. The white "x's" indicate the locations where the  $n = 1, 0$ , and  $-1$  resonances cross the  $v_\perp = 0$  axis (see Roberg-Clark et al. 2019), and the black circles plot constant energy curves in the wave frame. Note that the electrons plotted in the core, halo, and strahl panels indicate the electrons that were initially in that category. As expected, the strahl electrons are significantly more scattered by the  $175^\circ$  wave than by the  $5^\circ$  wave, and the total distribution contains significantly fewer anti-sunward moving electrons. In the case of the  $65^\circ$  wave, the scattering of the strahl is more symmetric. There is reduced flux in the parallel (anti-sunward) direction, and broad flux peaks at pitch angles around  $30^\circ$ . In addition, the core is more strongly heated in the interaction with oblique waves. In comparing the scattering observed for the  $5^\circ$  and  $175^\circ$  waves to that seen for the  $65^\circ$  wave, it is important to note that the wave amplitude of  $20$  mV m<sup>-1</sup>, based on observations of oblique waves, was used for all wave angles. Observations at 1 au, however, have found only small amplitude ( $<1$  mV m<sup>-1</sup>) waves at parallel angles (Lacombe et al. 2014; Stansby et al. 2016; Tong et al. 2019). The final distributions shown for the  $5^\circ$  and  $175^\circ$  waves, therefore, greatly overestimate the potential impact of parallel propagating waves at  $\sim 1$  au.

The comparable results for single waves inside 0.3 au are shown in Figure 3(b) (same format and same color bar as Figure 3(a)). Because the halo is only a very small component of the electron population, only core and strahl are included in the initial distributions (based on Halekas et al. 2020a). Another key difference is that large amplitude parallel propagating waves and sunward propagating waves are observed inside 0.3 au; therefore, the results for  $5^\circ$  and  $175^\circ$  waves represent possible scattering processes. Some features are seen at both radial distances, including the decrease in fluxes along the magnetic field for all wave angles and the clear energy dependent cutoff in the scattering beyond  $90^\circ$  pitch angles in the  $175^\circ$  wave angle case. For the 0.3 au parameters, the core electrons are heated, especially for the  $65^\circ$  wave, and population centroid moves to the location of where the  $n = 0$  (Landau resonance) intersects the  $v_\perp = 0$  axis. For the  $65^\circ$  wave, there is strong scattering beyond  $90^\circ$  pitch angle along the constant energy circle in the wave frame at  $\sim 2$  keV. The energy dependence of the scattering is clearly seen in the 0.3 au figures; similar features were seen in the PSP observations (Cattell et al. 2021b).

The role of whistler waves is more accurately modeled using a group of wave packets, as can be seen in the examples in Figure 1. Figure 4 (in the same format as Figure 3) plots the results of the interactions with wave packets centered at  $0^\circ$  and  $65^\circ$  for 1 au, and  $0^\circ$ ,  $65^\circ$ , and  $180^\circ$  for 0.3 au. Comparing the final distributions for the single wave cases to the packet cases indicates that the interaction with a single wave results in more energization and/or scattering; however, some similar features can be seen. For the near parallel cases, both have peaks in the flux at an angle off parallel; for the packet, this is seen in both the negative and positive directions. The parallel packet case has constant energy (in the wave frame) enhancements at high energies for  $V_z > 0$  (clearly visible in the strahl panel), which extend to lower energies in the packet case as would be



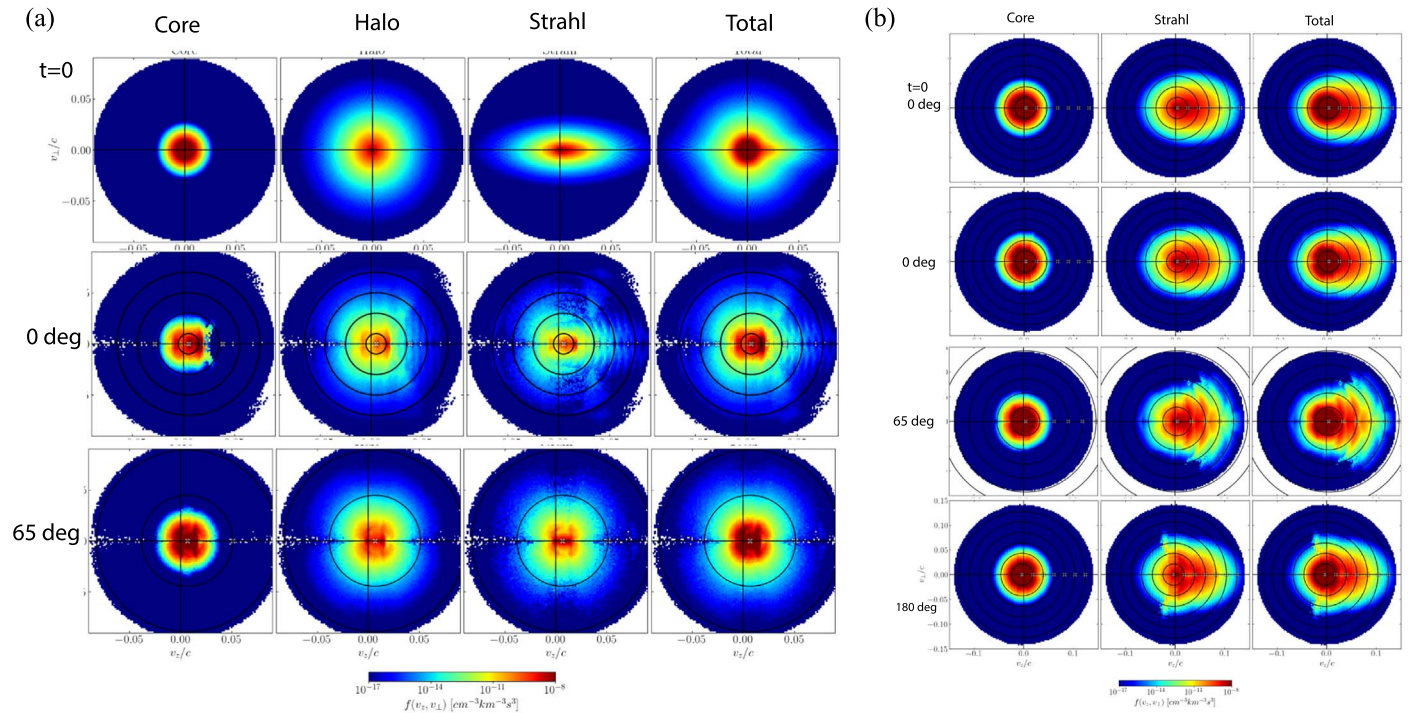
**Figure 3.** (a) Interaction of solar wind electron distributions at 1 au with single whistler wave. Top panels show the initial distributions. The next panels show the distributions after interacting with an almost parallel (in the direction of strahl), antiparallel (opposed to the strahl), and very oblique wave for 60 wave periods. The white x's indicate the location where the  $n = -1, 0,$  and  $1$  resonances intersect  $v_{\perp} = 0$ . The black circles plot constant energy in the wave frame. (b) Interaction of solar wind electron distributions at 0.3 au with single whistler wave. The top panel shows the initial distributions for core, strahl, and total distributions at  $t = 0$ . The next panels show the distributions after interacting with an almost parallel (in the direction of strahl), antiparallel (opposed to the strahl), and very oblique wave for 60 wave periods. The white x's indicate the location where the  $n = -1, 0,$  and  $1$  resonances intersect  $v_{\perp} = 0$ . The black circles plot constant energy in the wave frame.

expected due to the fact that there are multiple resonant energies in the packet. For the oblique wave cases, both show minima in the magnetic field-aligned and anti-field-aligned directions, most clearly for the single wave case. Both the  $0^{\circ}$  and  $65^{\circ}$  packets have a region of enhanced flux at a constant parallel velocity (most obvious in the higher density core). In addition, the  $65^{\circ}$  packet and single wave cases have very prominent horn-like elements at higher energies; the  $0^{\circ}$  waves show these horns, most clearly in the 1 au case. These structures are comparable to the multiple horns described by Roberg-Clark et al. (2019) and attributed to higher order resonances. Similar features were seen at early times in the simulations of Micera et al. (2020) when oblique whistlers were growing. The  $180^{\circ}$  packet case was only run for 0.3 au because no sunward propagating whistlers have been found at 1 au. The  $180^{\circ}$  packet shows energy dependent features similar to the  $175^{\circ}$  single wave, but electrons are not scattered as significantly. The most significant scattering of the strahl and heating of the core is observed in interactions with the oblique waves. The evolution of these and other features can be clearly seen in the animations, which plot the distributions versus time.

To more clearly illuminate the role of trapping in different resonances, as well as scattering and energization for different initial pitch angles and energies, we utilized multiple time series videos examining specific initial conditions, such as ones looking at restricted energy ranges and pitch angles or initial propagation directions. These reveal the very complex

interactions of electrons with large amplitude waves. Trapping and de-trapping of electrons in different resonances occurs, most likely in accordance with the resonance trapping width of each resonance. Figure 5(a), which plots the (color coded) trajectories in velocity space of electrons initially moving opposite to the wave parallel phase velocity with different speeds (panels A1, B1, C1, and D1) and their corresponding histograms (A2, B2, C2, and D2). This provides a visualization of trapping for the cases of single waves ( $5^{\circ}$  and  $65^{\circ}$ ) and packets ( $0^{\circ}$  and  $65^{\circ}$ ). The vertical dashed lines indicate the resonance surfaces; the dotted elliptical curves are the lines of constant energy surface in the wave frame. The bright regions occur where the particles remain for longer times during the simulation period, indicative of trapping. Figure 5(b) shows animations for the single wave cases (on the left) similar to Figure 5(a) panels A1 and C1. The right-hand animations are for wave packets, similar to panels B1 and D1. Note that Figure 5(a) only shows the initially antiparallel particles, while Figure 5(b) includes particles initially both parallel and antiparallel to the waves. The amount of scattering and energization is very dependent on the initial electron energy and pitch angles, as well as the wave properties.

As discussed in the 1, simple arguments based on the resonance conditions imply that electrons propagating in the same direction as a parallel propagating wave will not interact strongly with the wave. The simulations show, however, that by  $\sim 6$  wave periods some of the highest energy ( $\sim 1300$  eV)



**Figure 4.** (a) Interaction of electrons with wave packets (same format as Figure 3(a)). (b) Interaction of wave packets with electrons at  $\sim 0.3$  au. Final time is 45 wave periods. Same format as Figure 3(b). An animation of the last three rows of this figure is available. The animation shows the  $0^\circ$ ,  $65^\circ$ , and  $180^\circ$  packet simulations from  $t$  (in wave periods) = 0.00–45.00. The real time duration of this animation is 38 s.

(An animation of this figure is available.)

electrons near  $90^\circ$  pitch angle are scattered so that their parallel velocity component is anti-sunward, and these electrons interact strongly with the wave. The interaction with the wave packets occurs more quickly for the electrons that are initially moving antiparallel to the wave; the highest energy electrons already scattered to all pitch angles by three wave periods, whereas, in the parallel case, this occurs by  $\sim$ five wave periods. For the  $65^\circ$  wave packet, the interaction with the electrons traveling in either direction occurs within a time comparable to that for the antiparallel electrons in the parallel propagating wave packet case ( $\sim$ three wave periods).

As expected for the  $0^\circ$  packet, the electrons with initial pitch angles near  $180^\circ$  are rapidly scattered. Some electrons are trapped in the  $n = 1$  resonance: for initial energies of  $\sim 300$  eV, the trapping is at pitch angles of  $\sim 50^\circ$  with energization up to  $\sim 700$  eV; and, for initial energies  $\sim 1000$  eV, the trapping is at  $\sim 60^\circ$ – $70^\circ$  with energization to  $\sim 1500$  eV. At the highest energies, the electrons experience alternate trapping and de-trapping. In contrast, the  $0^\circ$  electrons lose energy and are only weakly scattered by the end of the simulation. Some electrons initially at  $\sim 90^\circ$  and  $\sim 1000$  eV are trapped in  $n = 0$  and the  $n = 1$  resonances. During the interaction with the  $65^\circ$  packets, electrons with all initial conditions are very rapidly scattered, with the response of the  $180^\circ$  particles slightly preceding those at  $0^\circ$  at all energies. There is evidence for trapping of some electrons in all three resonances  $n = -1, 0, +1$ ). The scattering results in a loss of particles with pitch angles along the magnetic field.

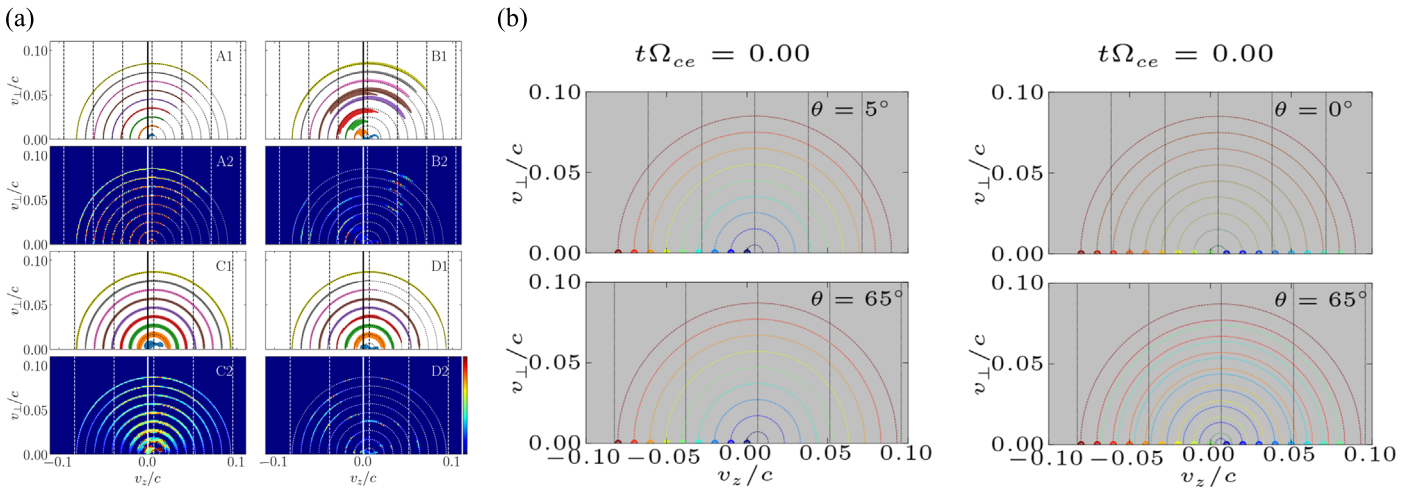
#### 4. Discussion and Conclusions

Results of a fully 3D relativistic particle tracing code with wave properties based on the narrowband whistler-mode waves

observed at  $\sim 1$  au by STEREO (Cattell et al. 2020) and inside 0.3 au by PSP (Cattell et al. 2021a), and initial electron distributions based on Wind data at 1 au (Wilson III et al. 2019) and the PSP data inside 0.3 au (Halekas et al. 2020a) show that solar wind electrons from core through strahl (energies from a few eV to a few keV) can be strongly scattered and/or energized. The whistlers scatter the strahl to produce the isotropic halo, as required to explain the observed strahl width and the changes in the relative densities of the strahl and halo with distance from the Sun, and the limitation of the electron heat flux. The conclusions are significant not only for the solar wind, but potentially also for other high beta astrophysical settings including the interstellar medium and intercluster medium.

Studies of electron acceleration both in the solar wind (Saito & Gary 2007a, 2007b) and in the Earth’s radiation belts (Tao et al. 2013) have demonstrated that the wave packet structure dramatically affects the acceleration and scattering of electrons. Comparison of our results for the single wave to those for wave packets indicate that, although some features are weakened in the packet cases, there are new scattering features observed only with packets. This is due to the existence of multiple resonances and resonant overlaps associated with the different frequencies in the packets.

Our particle tracing simulations using parameters appropriate for inside  $\sim 0.3$  au show that both the highly oblique and the sunward propagating parallel whistler-mode waves rapidly scatter the strahl to produce the hotter more isotropic halo, and to reduce the heat flux carried by the strahl electrons. Oblique waves more significantly scatter the strahl, consistent with the study of Halekas et al. (2020b), which showed that the electron heat flux was constrained by the oblique heat flux fan instability. Features seen in the simulations, including peaks



**Figure 5.** (a) Traces of nine electron trajectories in the entire simulation period for 1 au parameters and their corresponding histograms. All particles are initially antiparallel to the wave ( $v_z < 0$ ). The initial speeds are 0; 0.01; 0.02; ...; 0.08 c, which correspond to 0; 26; 102; ...; 1643 eV. Panels A1 and A2 show the interaction with a single  $5^\circ$  whistler. Panels B1 and B2 show the interaction with a  $0^\circ$  whistler packet. Panels C1 and C2 show the interaction with a single  $65^\circ$  whistler. Panels D1 and D2 show the interaction with a  $65^\circ$  whistler packet. The vertical dashed lines indicate the resonance surfaces; the dotted elliptical curves are the lines of constant energy surface in the wave frame. (b) shows animations for the single wave cases (on the left) similar to Figure 5(a) panels A1 and C1. The right-hand animations are for wave packets, similar to panels B1 and D1. Note that Figure 5(a) only shows the initially antiparallel particles, while Figure 5(b) includes particles initially both parallel and antiparallel to the waves.

(An animation of this figure is available.)

at angles to the magnetic field in some energies, scattering past  $90^\circ$ , energy dependent scattering and evidence for higher order resonances, are consistent with the direct observations of electron scattering and energization by narrowband whistler-mode waves using the PSP wave and electron observations (Cattell et al. 2021b). The core heating seen in our simulations is also seen when the large amplitude narrowband whistlers are observed (Cattell et al. 2021a), but not in studies of core electron temperature that are not constrained to times with waves. In addition, results are consistent with observed changes in the electron distributions made by both PSP and Helios (Maksimovic et al. 2005; Halekas et al. 2020a, 2020b), including the decreased strahl and increased halo densities, and the increase in pitch angle width of the strahl.

We can compare our results with two PIC simulations that examined the interaction of whistlers with electrons. Roberg-Clark et al. (2019) modeled this process in the context of solar flares, with an energetic outflowing electron kappa distribution and a cold return current population. Large amplitude oblique whistlers, propagating first with and then against the heat flux, and electron acoustic waves were excited. The whistler power peaked at highly oblique angles with amplitudes comparable to those observed in the PSP and STEREO data. The electrons were rapidly scattered with multiple energy dependent horn-like features similar to those we observed in the particle tracing for the oblique wave case at 0.3 au. The simulations of Micera et al. (2020) were initialized with core and strahl distributions based on the same PSP measurements (Halekas et al. 2020a) that we utilized. They found that initially highly oblique whistler waves were excited, and scattered the strahl to produce a single horn-like feature. At later times, parallel whistlers were excited, producing additional scattering that further isotropized the electron distributions. Both PIC studies discuss the time evolution of the role different resonances and the importance of nonlinear interactions with the large amplitude waves.

The changes seen in the electron distributions for the 1 au simulations are most directly applicable to understanding the

observed radial evolution around and beyond 1 au. The ratio of halo to strahl density continues to increase with radial distance (Štverák et al. 2009), and a clear strahl is often absent outside 1 au (Graham et al. 2017). This is consistent with our simulation results that show that scattering by oblique waves with properties based on those observed at 1 au results in an almost isotropic distribution.

In summary, the results of our particle tracing simulations with parameters based on observations of electrons and waves inside 0.3 au and at 1 au provide strong evidence for the central role of oblique whistler-mode waves in the evolution of solar wind electrons. The whistler scattering of the strahl electrons produces the halo and limits the electron heat flux. Kinetic effects of resonant interactions are revealed through the trapping of particles on the constant energy surfaces. This could be further studied and characterized through the resonance trapping width structures of whistler packets. Our conclusions are also applicable to other high beta astrophysical plasmas.

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